

Ingredients

Possible individuals

$A = \{ \text{Judith}, \text{Michael}, \dots \}$

Possible situations

$S = \{ s25, s37, s219, \dots \}$

Relations between them

Lexical entries:

for names:

$[[\text{Judith}]] = \text{Judith}$

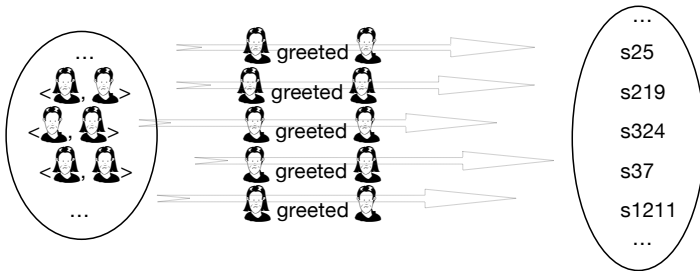
$[[\text{Michael}]] = \text{Michael}$

in general: $[[\text{Name}]] = \text{a member of the set A (possible individuals)}$

for verbs:

$[[\text{begrüßte}]] = \{ \langle \text{Judith}, \text{Michael}, s25 \rangle, \langle \text{Judith}, \text{Michael}, s37 \rangle, \langle \text{Judith}, \text{Michael}, s219 \rangle, \dots \}$

“draw an arrow from a pair of individuals to a situation, whenever the situation is such that the first member of the pair greeted the second one”



in general: $[[\text{Vi}]] = R$, where R is a subset of $A \times S$

$[[\text{Vt}]] = R$, where R is a subset of $A \times A \times S$

Syntactic structure

Semantic composition rules

- Composition Rule One
- Composition Rule Two

The composition rules tell us how to combine (two) meanings of constituents that we already know to a new meaning, the meaning of the constituent consisting of those constituents.

Composition Rule Two tells us how to combine sets of triples (that are subsets of $A \times A \times S$) with individuals. We can use it to combine transitive verb meanings and object meanings (if the object is a proper name) to obtain VP meanings.

Composition Rule One tells us how to combine sets of pairs (that are subsets of $A \times S$) with individuals. We can use it to combine VP meanings with subject meanings (if the subject is a proper name) to obtain sentence meanings.

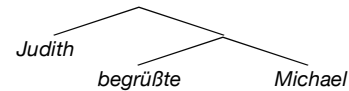
Set theoretic principles

- Comprehension Principle

Sentence meanings

Now we will use those ingredients to try to derive the meaning of sentences, f.i. *Judith begrüßte Michael*. i.e. we want to find out what $[[\text{Judith begrüßte Michael}]]$ is.

Lets assume that syntax gives us the following structure:



First we look up the meaning of the words in our lexicon:

$[[\text{Judith}]] = \text{Judith}$, $[[\text{Michael}]] = \text{Michael}$, $[[\text{begrüßte}]] = \{ \langle a, b, s \rangle \mid a \text{ greeted } b \text{ in } s \}$

Now we see that the VP tree matches composition rule two, since $[[\text{Michael}]]$ is a member of A and $[[\text{begrüßte}]]$ is a subset of $A \times A \times S$. Hence we know how to put them together and can derive the VP meaning: $[[\text{begrüßte Michael}]] = \{ \langle a, s \rangle \mid a \text{ greeted } \text{Michael} \text{ in } s \}$

Now composition rule one tells us what to do with relations that are subsets of $A \times S$ and individuals, so we can put the VP meaning together with the subject meaning: $[[\text{Judith begrüßte Michael}]] = \{ s \mid \text{Judith} \text{ greeted } \text{Michael} \text{ in } s \}$.